

4.3 Multiplying and Dividing Monomials

(pp. 128-13)

Name: _____

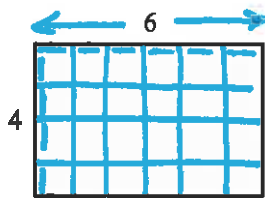
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Learning Goals: I will learn to

- use multiple strategies to multiply and divide monomials
- solve problems involving multiplication and division of monomials

An area model can be used to illustrate multiplication.

Example: 6×4



Area = 6×4
 $= 24 \text{ units}^2$

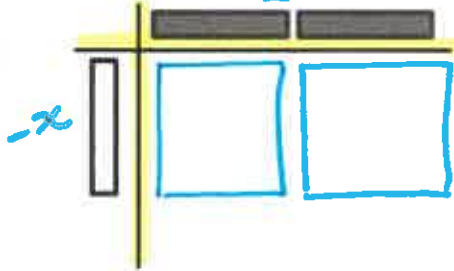
Similarly, we can use algebra tiles to model multiplication of monomials.

Examples:

a) $2x(3) = 6x$



b) $2x(-x) = -2x^2$



c) $-2x(2y) = -4xy$



To multiply two monomials:

multiply the coefficients
 and use exponent rules to multiply the variables

Remember...

<p>pos \times pos = pos</p> <p>neg \times neg = pos</p> <p>pos \times neg = neg</p> <p>neg \times pos = neg</p>	<p>Product of Powers</p> <p>$a^m \times a^n = a^{m+n}$</p>
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Develop Understanding

Example 1: Multiply Monomials (p. 129)

Multiply each pair of monomials.

$$\begin{aligned} \text{a) } (3x)(2x) \\ &= \underline{(3)(2)(x)(x)} \\ &= 6x^2 \end{aligned}$$

$$\begin{aligned} \text{b) } (3x)(-2x) \\ &= \underline{(3)(-2)(x)(x)} \\ &= -6x^2 \end{aligned}$$

$$\begin{aligned} \text{c) } (3x)(2y) \\ &= \underline{(3)(2)(x)(y)} \\ &= 6xy \end{aligned}$$

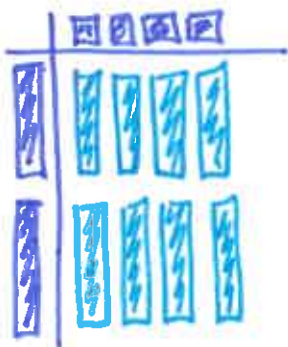
Show You Know

Multiply each pair of monomials.

$$\text{a) } 4(2x) = 8x$$

$$\text{b) } (-3x)(5x) = -15x^2$$

$$\text{c) } (5y)(4x) = 20xy$$



We can use algebra tiles to model **division of monomials** (multiplication in reverse).

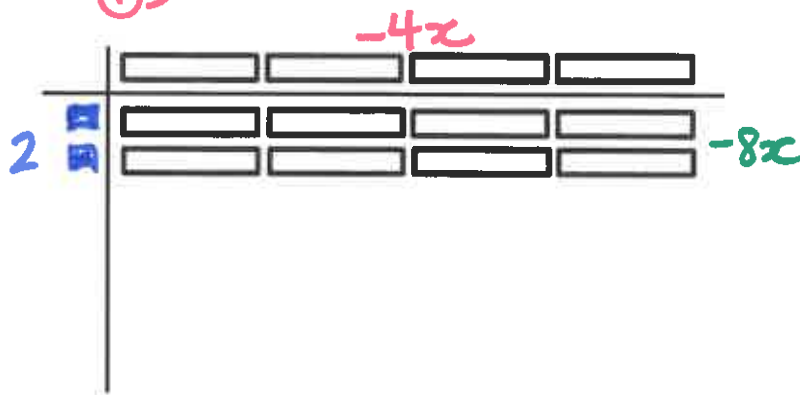
- ① 1. Place tiles representing the denominator along one edge.
- ② 2. Place tiles representing the numerator inside the grid (match to the known edge).
- ③ 3. Place tiles representing the quotient (answer) along the remaining edge.

Examples:

a) $\frac{-6x^2}{2x} = -3x$



b) $\frac{-8x}{-4x} = 2$



To divide two monomials:

divide the coefficients
and use exponent rules to divide the variables

Remember...

<p>pos ÷ pos = pos</p> <p>neg ÷ neg = pos</p> <p>pos ÷ neg = neg</p> <p>neg ÷ pos = neg</p>	<p>Quotient of Powers</p> $\frac{a^m}{a^n} = a^{m-n}$
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Example 2: Divide Monomials (p. 130)

Divide each pair of monomials.

a) $(8x^2) \div (4x) = 2x$

b) $\frac{-4xy}{2y} = \left(\frac{-4}{2}\right)\left(\frac{x}{1}\right)\left(\frac{\cancel{y}}{\cancel{y}}\right)$
 $= -2x$

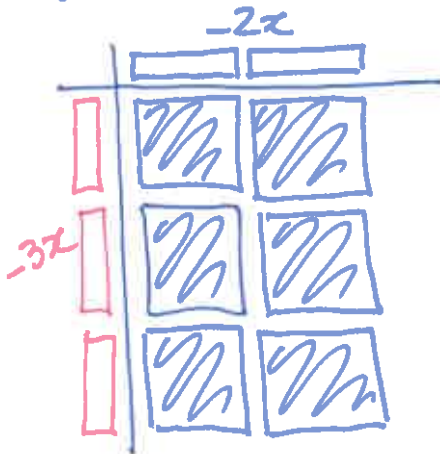


Show You Know

Divide each pair of monomials.

a) $(6x^2) \div (-2x) = -3x$

* draw tiles



b) $\frac{10xy}{5y} = \left(\frac{10}{5}\right)\left(\frac{x}{1}\right)\left(\frac{\cancel{y}}{\cancel{y}}\right)$
 $= 2x$

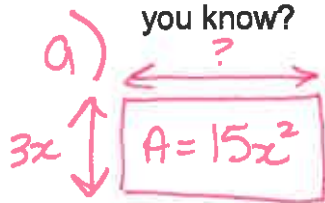
c) $\frac{-12xy}{-3x} = \left(\frac{-12}{-3}\right)\left(\frac{\cancel{x}}{\cancel{x}}\right)\left(\frac{y}{1}\right)$
 $= 4y$

Example 3: Apply Monomial Division (p. 131) *area*

The area of a rectangle is given by the expression $15x^2$. The width of the rectangle is represented by $3x$. *width*

a) What is the length of the rectangle in terms of x ?

b) Choose a value for x . Draw the rectangle to scale. Is the area of the rectangle $15x^2$? How do you know?

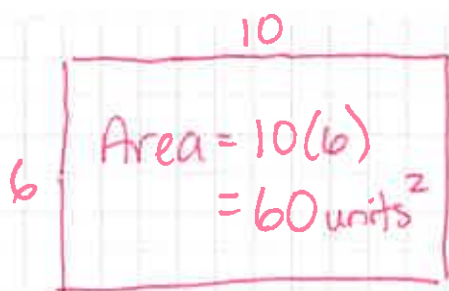


$$\frac{A}{w} = \frac{l \cdot w}{w}$$

$$\frac{A}{w} = l$$

$$\Rightarrow \frac{15x^2}{3x} = 5x$$

the length is $5x$



$$\begin{aligned} A &= 15x^2 \\ &= 15(2^2) \\ &= 15(4) = 60 \text{ units}^2 \end{aligned}$$

b) choose $x = 2$

→ length = $5x$
 $= 5(2)$
 $= 10$

↘ width = $3x$
 $= 3(2)$
 $= 6$

Key Ideas

- You can use a model, such as algebra tiles, to represent the multiplication and division of monomials.
- To multiply two monomials, multiply the coefficients and use the exponent rules to multiply the variables.
- To divide two monomials, divide the coefficients and use the exponent rules to divide the variables.